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Fifth Semester B.E. Degree Examination, June/July 2023

Electromagnetic Waves

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Derive the expression for Electric Field due to line charge of infinite length. (08 Marks)
- b. Find the force on $100 \mu\text{C}$ charge at $(0, 0, 3)\text{m}$, if four like charges of $20 \mu\text{C}$ are located on the x and y axis at $\pm 4\text{m}$. (06 Marks)
- c. Determine Electric Field at origin due to charge at $6.44 \times 10^{-9}\text{C}$ located at $(4, 2, -3)\text{m}$ in Cartesian coordinate system. (06 Marks)

OR

- 2 a. A charge lies in the $Z = -3\text{m}$ plane in the form of a square sheet defined by $-2 \leq x \leq 2$, $-2 \leq y \leq 2$ m with $\rho_s = 2(x^2 + y^2 + 9)^{3/2}$ nc. Find Electric field at origin. (07 Marks)
- b. Three negative charges $Q_1 = -1 \mu\text{C}$, $Q_2 = -2 \mu\text{C}$, $Q_3 = -3 \mu\text{C}$ are placed at the corners of an equilateral triangle. If length of each side is 1m, find magnitude and direction of EF at a point bisecting line between the charge Q_2 and Q_3 . (08 Marks)
- c. Derive the expression for Electric field intensity due to several point charges. (05 Marks)

Module-2

- 3 a. A charge Q is uniformly distributed in a square ring of side l. Find E and V at centre of the ring. (08 Marks)
- b. Determine work done in carrying a charge of -2C from $(2, 1, -1)$ to $(8, 2, -1)$ in Electric field $E = y\hat{a}_x + x\hat{a}_y$ considering the path along parabola $x = 2y^2$. (05 Marks)
- c. State and prove Gauss divergence theorem. (07 Marks)

OR

- 4 a. A point charge $Q = 90 \mu\text{C}$ is located at origin and these are two uniformly surface charge density distribution $-8 \mu\text{C}/\text{m}^2$ at $r = 1\text{m}$ and $4.5 \mu\text{C}/\text{m}^2$ at $r = 2$. Find \bar{D} everywhere. (08 Marks)
- b. Given $D = 5r \hat{a}_r$ C/m². Determine whether divergence theorem holds good for shell region enclosed by spherical surface at $r = a$ and $r = b$ ($b > a$) centred at origin. (07 Marks)
- c. Find the potential and volume charge density at $P(0.5, 1.5, 1)\text{m}$ in free space given $V = 2x^2 - y^2 - z^2$. (05 Marks)

Module-3

- 5 a. Let $V = A \ln \left[\frac{B(1 - \cos \theta)}{1 + \cos \theta} \right]$
 - i) Show that V satisfies Laplace equation in spherical coordinates.
 - ii) Find A and B, so that $V = 100 \text{V}$ and $E = 500$ at $r = 5\text{cm}$, $\theta = 90^\circ$, $\phi = 60^\circ$. (08 Marks)
- b. State and explain Stokes theorem. (04 Marks)
- c. Determine whether or not the following potential satisfy Laplace equation :
 - i) $V = r \cos \phi + z$
 - ii) $V = x^2 - y^2 + z^2$ (08 Marks)

OR

- 6 a. Find the magnetic field intensity at P for the Fig.Q6(a).

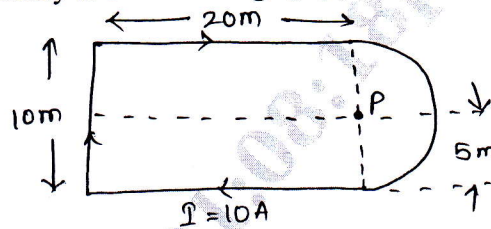


Fig.Q6(a)

- (08 Marks)
- b. There exist a potential of $V = -2.5V$ on the conductor of $0.02m$ and $V = 15V$ at $r = 0.35m$. Determine E and D by solving Laplace equation in spherical coordinates. (07 Marks)
- c. If the magnetic field intensity in region $H = (3y - 2)\hat{a}_z + 2x\hat{a}_y$. Find current density. (05 Marks)

Module-4

- 7 a. For region1, $\mu_1 = 4\mu$ H/m and for region2, $\mu_2 = 6\mu$ H/m. The regions are separated by $Z = 0$ plane. The surface current density at the boundary is $K = 100\hat{a}_x$ A/m. Find B_2 if $B_1 = 2\hat{a}_x - 3\hat{a}_y + \hat{a}_z$ mT for $Z = 0$. (08 Marks)
- b. A circular conducting loop of radius $40cm$ lies in xy plane and has a resistance of 20Ω . If magnetic flux density is $B = 0.2 \cos(500t)\hat{a}_x + 0.75\sin(400t)\hat{a}_y + 1.2\cos(314t)\hat{a}_z$. Find induced current in Loop. (07 Marks)
- c. Explain Lorentz force equation. (05 Marks)

OR

- 8 a. A conductor of length $2.5m$ in $Z = 0$ and $x = 4m$ carries a current of $12A$ in $-\hat{a}_y$ direction. Calculate uniform flux density in region, if force on the conductor is $12 \times 10^{-2} N$ in direction by $\left[\frac{-\hat{a}_x + \hat{a}_z}{\sqrt{2}} \right]$. (07 Marks)
- b. Explain Magnetization and Permeability. (07 Marks)
- c. Explain force between differential current elements with equation. (06 Marks)

Module-5

- 9 a. Given $H = H_m e^{j(\omega t + \beta z)} \hat{a}_x$ A/m in free space. Find E. (07 Marks)
- b. Derive the wave equation for vector E and H field in conducting medium. (08 Marks)
- c. Prove that $\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$. (05 Marks)

OR

- 10 a. Discuss the propagation of uniform plane wave in good conductor and explain skin depth. (08 Marks)
- b. Determine $\alpha, \beta, \gamma, v, \lambda, \eta$ for damp soil at frequency of $1 MHz$ given that $\epsilon_r = 12, \mu_r = 1$, and $\sigma = 20m \text{ } \Omega/m$. (05 Marks)
- c. Find the Amplitude of displacement current density in free space within large power distribution
 $H = 10^6 \cos(377t + 1.256 \times 10^{-6}z)\hat{a}_y$ (07 Marks)
